Representation of softness characteristics for active robotic in-hand exploration of objects



Objectives:

 Implementation of a volumetric representation (spatial discrimination of heterogenous objects) of the softness characteristics of objects;

 The elementary spatial representation of perceived softness is described as a probabilistic combination of softness description of reference sample materials;

•The perceived softness is represented based on previous experience and knowledge, to incorporate uncertain and to be progressively updated;

Object softness volumetric representation:

→Volumetric representation framework

Volumetric discrete grid;

•The grid divides the workspace into equally sized voxels;

·Edges are aligned with the world reference frame { W };

→Softness categories representation

 Characteristic signature of each of the reference materials, m, is modeled by:

$$C_P^m(C_D) = a_1^m C_D^{\frac{3}{2}} + a_2^m \qquad C_P^m(C_A) = a_3^m C_A^{\frac{3}{2}} + a_4^m$$

•The curve parameters (a_1 , a_2 , a_3 , a_4) for each reference material, m, can be learnt by performing several human demonstrations of unaxial palpation of the test materials.

-For each voxel *I*, the set D'_{n-1} contains the *n*-1 measurements influencing that voxel

 $p(m_l|\mathbf{D}_n^l) = \beta_1\beta_2\prod p(m_l|\mathbf{D}_j^l) = \beta_1\beta_2 p(m_l|\mathbf{M}_i^l)p(m_l|\mathbf{D}_{n-1}^l)$

•The knowledge about the softness of a voxel, m_{l} , after n batches of measurements is modeled trough a probability distribution function:

 $p(m_l | \mathbf{D}_n^l) = m_l \varepsilon \{ \text{Material}_1, \text{Material}_2, \dots, \text{Material}_M \}$

•Each of the *M* softness categories is specified by a sample of a representing reference material

•Assuming that the data samples C_{P}^{m} are statistically independent and the statistical distribution of each sample C_{P}^{m} follows a Gaussian distribution.

$$p(C_{P,i}^{m}|(a_{1}^{m},a_{2}^{m})) = \frac{1}{2\pi\sqrt{\sigma}}e^{-\frac{(C_{P,k}^{m}-(a_{1}^{m}C_{D,i}^{k}+a_{2}^{m}))^{2}}{2\sigma^{2}}} \qquad p(C_{P,i}^{m}|(a_{3}^{m},a_{4}^{m})) = \frac{1}{2\pi\sqrt{\sigma}}e^{-\frac{(C_{P,k}^{m}-(a_{3}^{m}C_{D,i}^{k}+a_{2}^{m}))^{2}}{2\sigma^{2}}}$$

•The parameters (a_1, a_2, a_3, a_4) for each reference material, *m*, are estimated by least square estimate

\rightarrow Volumetric representation update

• $p(m_l|\mathbf{M}_i^t)$ converts the measurements $\mathbf{M}_k = (\mathbf{C}_{P}, \mathbf{C}_{A}, \mathbf{C}_{D})$ in estimation of softness values m_l of voxel *l*.

• $p(m_l|\mathbf{M}_i^l)$ is determined by $p(m_l|\mathbf{M}_i^l) = \frac{P(\mathbf{M}_i^l,m_l)}{p(\mathbf{M}_i)} = \frac{p(\mathbf{M}_i^l|m_l)p(m_l)}{\sum_m p(\mathbf{M}_i^l|m_l)p(m)}$

ISR – Coimbra

